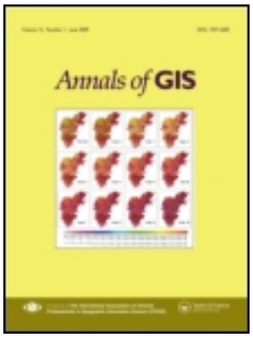


Taylor & Francis
Taylor & Francis Group

Geographic Information Sciences

A Journal of the Association of Chinese Professionals in Geographic Information Systems

ISSN: 1082-4006 (Print) (Online) Journal homepage: http://www.tandfonline.com/loi/tagi19

Multiscale Analysis of Landscape Heterogeneity: Scale Variance and Pattern Metrics

Jianguo Wu , Dennis E. Jelinski , Matt Luck & Paul T. Tueller

To cite this article: Jianguo Wu , Dennis E. Jelinski , Matt Luck & Paul T. Tueller (2000) Multiscale Analysis of Landscape Heterogeneity: Scale Variance and Pattern Metrics, Geographic Information Sciences, 6:1, 6-19, DOI: 10.1080/10824000009480529

To link to this article: http://dx.doi.org/10.1080/10824000009480529

Published online: 12 Aug 2009.

Submit your article to this journal

Article views: 1567

View related articles

Citing articles: 28 View citing articles

Full Terms & Conditions of access and use can be found at
http://www.tandfonline.com/action/journalInformation?journalCode=tagi19

Download by: [University of North Texas] **Date:** 28 December 2016, At: 13:49

Multiscale Analysis of Landscape Heterogeneity: Scale Variance and Pattern Metrics

Jianguo Wu*, Dennis E. Jelinski§, Matt Luck*, and Paul T. Tueller†

*Department of Life Sciences, Arizona State University-West
P. O. Box 37100, Phoenix, Arizona 85069, USA
§School of Environmental Studies and Department of Geography
Queen's University, Kingston, Ontario, K7L 3N6, Canada
'Department of Environmental and Resource Sciences
University of Nevada, Reno, NV 89557, USA

Abstract
A major goal of landscape ecology is to understand the formation, dynamics, and maintenance of spatial heterogeneity. Spatial heterogeneity is the most fundamental characteristic of all landscapes, and scale multiplicity is inherent in spatial heterogeneity. Thus, multiscale analysis is imperative for understanding the structure, function and dynamics of landscapes. Although a number of methods have been used for multiscale analysis in landscape ecology since the 1980s, the effectiveness of many of them, including some commonly used ones, is not clear or questionable. In this paper, we discuss two approaches to multiscale analysis of landscape heterogeneity: the direct and indirect approaches. We will focus on scale variance and semivariance methods in the first approach and **17** landscape metrics in the second. The results show that scale variance is potentially a powerful method to detect and describe multiple-scale structures of landscapes, while semivariance analysis may often fail to do so especially if landscape variability is dominant at broad scales over fine scales. Landscape metrics respond to changing grain size rather differently, and these changes are reflective of the modifiable areal unit problem as well as multiple-scale structures in landscape pattern. Interestingly, some metrics (e.g., the number of patches, patch density, total edge, edge density, mean patch size, patch size coefficient of variation) exhibit consistent, predictable patterns over a wide range of grain sizes, whereas others (e.g., patch diversity, contagion, landscape fractal dimension) have nonlinear response curves. The two approaches to multiple-scale analysis are complementary, and their pros and cons still need to be further investigated systematically.

I. INTRODUCTION

Spatial heterogeneity is ubiquitous in nature across all scales, and its formation and interactions with ecological processes are the central issue in landscape ecology. It is intriguing, however, to note that the spatial dimension has long been ignored or purposefully avoided in ecology given that all ecological phenomena take place in spatially heterogeneous environments and that the relationship between organisms and their environment is the very subject of ecology. This ignorance has had much to do with the background assumption of balance of nature and the traditional equilibrium paradigm in ecology (Wu and Loucks 1995). Besides, several reasons are attributable to the slow progress in spatial ecology, i.e., the spatially explicit study of the interactions between pattern and process in ecological systems.

The first is the lack of recognition of the importance of the interactions between space and other factors that together give rise to ecological patterns or processes. Although plant ecologists have long been interested in the geographical distribution of communities since the 1800s, the interactions between space and ecological processes have not been well studied. It was not until the 1980s that the interaction among pattern, process and scale began to occupy a central place in ecological studies, especially, with developments in patch dynamics and hierarchy theory (O'Neill et al. 1986, Levin 1992, Wu and Levin 1994, Wu and Loucks 1995). The second reason concerns the lack of effective statistical and modeling methods for studying spatial phenomena. Many, if not most, statistical methods traditionally used in ecological research assume the independence of the observations. Spatial autocorrelation and spatial dependence, however, are extremely common for ecological variables (Legendre 1993), which violate this fundamental assumption, thus impairing methods that are based on it. Although there are ways of removing spatial structure in data, doing so may not be ecologically sensible if space is considered an integral part of ecological phenomena. Only in recent years, new methods in spatial statistics (particularly geostatistics) began to be introduced in ecology to alleviate this problem (e.g.,

1082-4006/99/0601-6$5.00
02000 The Association of Chinese Professionals in Geographic Information Systems (Abroad)

Legendre and Fortin 1989, Robertson 1987, Rossi et al. 1992, Legendre 1993).

The third reason has to do with the insufficient capacity of computers. Spatial analysis usually requires enormous memory space, high computing speed, and complex software development. All of these have been limiting factors in much of the history of ecology as well as statistics. Fortunately, these problems are now greatly eased with rapid advances in computer technologies, including the availability of GIS. The fourth reason involves problems arising from data aggregation, which often lead to error propagation and controversial results. Ecological studies frequently use area-based information, derived from field surveys, aerial photography, or remote sensing sources. The boundaries of the areal units, however, are usually arbitrary. As Greig-Smith (1983) pointed out, there is an "element of subjectivity in sampling procedure because the boundaries within which a set of samples is taken are fixed by the ecologist on the basis of his judgment of what can suitably be described as one unit for the purpose at hand." The arbitrariness in the definition of areal units can affect the results of a number of statistical analyses. This problem has been known as the modifiable areal unit problem (MAUP) in the geographical literature (Openshaw 1984), and has recently been studied in the context of landscape ecology (Wu and Jelinski 1995, Jelinski and Wu 1996). MAUP consists of two closely related aspects: the scale problem and the zoning problem. The scale problem concerns changes in the results of spatial analysis with changing scale (usually grain size), whereas the zoning problem results from the variations of the results of spatial analysis due to different zoning systems or spatial configurations of areal units at the same scale. The studies of MAUP have shown that a wide variety of spatial analyses and simulation models are susceptible to both scale and zoning problems (Jelinski and Wu 1996, Marceau 1999). As a result, the composition of a landscape (e.g., patches, gaps, edges, and corridors) may also vary with changing grain size and extent.

To understand the dynamics of patterns and processes and their interactions in a heterogeneous landscape, one must be able to accurately quantify the spatial pattern and its temporal changes of the landscape. Recent studies have shown that one of the most important and universal characteristics of spatial heterogeneity is its scale multiplicity in space (e.g., Miller 1978, Kolasa and Pickett 1991, Wu and Loucks 1995, Cullinan et al. 1997, Werner 1999). This scale multiplicity of landscapes has several important ecological implications: (1) landscapes may be, though not necessarily, hierarchically structured; (2) landscapes exhibit distinctive spatial patterns at different scales which mag be caused by different processes, and thus the scale of observation significantly influences what is to be observed; (3) understanding landscape functioning requires a multiple-scale characterization of spatial pattern and processes, and single-scale descriptions are doomed to be partial and misleading; and (4) models developed at one particular scale are not likely to apply at other scales, thus we need to either link models developed at different scales, or develop multiple-scaled or hierarchically structured models.

The process of extrapolating or translating information from one scale to another, scaling, undoubtedly is a fundamental challenge in both theory and practice across all earth sciences. In particular, scaling is essential for addressing a wide range of ecological and environmental problems concerning biodiversity loss and global change in part because most ecological studies to date have been carried out at very local scales in both time and space (van Gardingen et al. 1997, Wu 1999). Scaling often is a difficult task due primarily to landscape heterogeneity and nonlinearity, and understanding the scale multiplicity in pattern and process is a key to the success of scaling (Wu 1999).

This paper, therefore, discusses two approaches to multiscale analysis of landscape pattern: the direct and indirect approaches. Specifically, we demonstrate how to use scale variance analysis and landscape metrics as methods for detecting and describing multiple-scale or hierarchical structures in landscapes. Through a series of analyses, we address several specific questions, including: Is scale variance effective in detecting multiple-scale patterns? How does it compare with semivariance? How do landscape metrics change over a broad range of grain sizes? Are these changes predictable? Which landscape indices are sensitive to multiple-scale structures?

11. TWO APPROACHES TO MULTISCALE ANALYSES

To quantify multiple-scale characteristics of landscapes, multiscale or hierarchical approaches must be employed. While a hierarchical approach is by definition multiple-scale, a multiple-scale approach is not necessarily hierarchical in the sense of the nested hierarchy (Wu 1999). It is worth noting that the term, "scale", here is used to denote the grain size and extent of a data set, not necessarily corresponding to the "characteristic scale" of landscape pattern or processes. We may distinguish between two general approaches to multiscale analyses: (1) the direct multiscale approach that uses inherently multiple-scale methods, and (2) the indirect multiscale approach that uses single-scale methods repeatedly at differ-

ent scales. Frequently used multi-scale methods in landscape ecology include semivariance analysis (Robertson and Gross 1994, Burrough 1995), wavelet analysis (Bradshaw and Spies 1992, Saunders et al. 1998), spectral analysis (Platt and Denman 1975, Ripley 1978), fractal analysis (Krummel 1987, Milne 1991, Nikora et al. 1999), lacunarity analysis (Plotnick et al. 1993, Henebry and Kux 1995), and blocking quadrat variance analysis (Greig-Smith 1983, Dale 1999). All these methods contain multiple-scale components in their mathematical formulation or procedures, and thus are either hierarchical or multiscaled.

On the other hand, the indirect approach to multiscale analyses can use methods that are designed for single-scale analysis, such as the wide variety of landscape metrics (e.g., diversity, contagion, perimeter-area ratios, spatial autocorrelation indices) as well as statistical measures (e.g., mean, variance, correlation or regression coefficients). The scale multiplicity in the indirect approach is realized by resampling the data at different scales, albeit grain or extent, and then repeatedly computing the metrics or statistical measures using the resampled data at different scales. One particular way of resampling data is to systematically aggregate the original fine-resolution data set and produce a hierarchically nested data set, which leads to a hierarchical analysis using single-scale methods. Note that hierarchical analysis does not have to assume, ***apriori,*** the existence of a hierarchical structure in the landscape under study, but can be used to detect it.

In general, there are two related but distinctive goals for conducting a multiscale analysis in a landscape ecological study. The first is to characterize the multiple-scale structure of a landscape. The second is to detect or identify "scale breaks" or hierarchical levels in the landscape which often can be studied as a spatially nested hierarchy (O'Neill et al. 1991, Wu and Loucks 1995, Wu 1999). In both cases, a better understanding is achieved of how spatial heterogeneity changes with scale. However, a description of landscape pattern at different scales may be necessary or desirable even if scale breaks do not exist or the landscape is not hierarchical. On the other hand, scale breaks often lead to the identification of characteristic scales of patterns which may frequently facilitate understanding underlying processes. **A** series of methods for analyzing landscape heterogeneity have been reviewed recently (e.g., Turner et al. 1991, Burrough 1995, Gustafson 1998, Dale 1999, Fortin 1999). In the following, we demonstrate two multiscale approaches with specific examples. In particular, we focus on the use of scale variance analysis and several landscape metrics as they are used in multiscale analysis.

111. MULTISCALE ANALYSES WITH SCALE VARIANCE

Scale variance analysis is a hierarchical analysis that was first developed by Moellering and Tobler (1972). The initial goal of the method was to determine the relative variability at each level in a known nested hierarchy, and to evaluate each level's relative, independent contribution to the total variability of the whole system. However, the use of scale variance analysis does not necessarily require or even assume the existence of a nested hierarchy in the landscape under study. To conduct scale variance analysis, one only needs to systematically aggregate spatial data by increasing grain size progressively so that a nested data hierarchy is formed (see Figure **1).** Each grain size is termed a "scale level" (Moellering and Tobler 1972). Most spatial data can be reconstructed hierarchically by resampling, then scale variance analysis can be applied (Moellering and Tobler 1972, Townshend and Justice 1990, Wu et al. 1994, Barnsley et al. 1997).

The statistical model of scale variance can be expressed as:

$$X_{ijk\cdots z} = \mu + \alpha_i + \beta_{ij} + \gamma_{ijk} + \cdots + \omega_{ijk\cdots z} \qquad (1)$$

where $X_{jk\ldots z}$ is the value of a spatial unit (e.g., a pixel) at the hierarchical level that corresponds to the finest grain size (scale level 6 in Figure 1), μ the grand mean over the entire data set, α_i the effect of the *a* level (scale level **1** in Figure 1), β_{ij} the effect of the β level (scale level 2 in Figure 1), γ_{ijk} the effect of the y level (scale level 3 in Figure 1), and $\omega_{ijk\ldots z}$ the effect of ω level (scale level 6 in Figure 1).

From the above model, the total variance of the landscape can be partitioned hierarchically at different grain sizes. Moellering and Tobler (1972) derived the scale variance components for a 3-level (*a*, β, γ) hierarchy as follows. First, the total variation of the system is expressed as the total sum of squares:

$$SS_{Total} = \sum_{i=1}^{I}\sum_{j=1}^{J_i}\sum_{k=1}^{K_{ij}}(X_{ijk} - \overline{X}_{\cdots})^2 \qquad (2)$$

where I is the number of *a* level units, J_i is the number of **b** level units in each ith *a* level unit, and K_{ij} is the number of y level units in each ij^{th} β level unit.

The total sum of squares is partitioned into different parts that are attributable to the various scale levels (here *a*, β, γ), so that

$$SS_{Total} = SS_{\alpha} + SS_{\beta} + SS_{\gamma}\,. \qquad (3)$$

SS_{α}, SS_{β}, and SS_{γ} are calculated based on the follow-

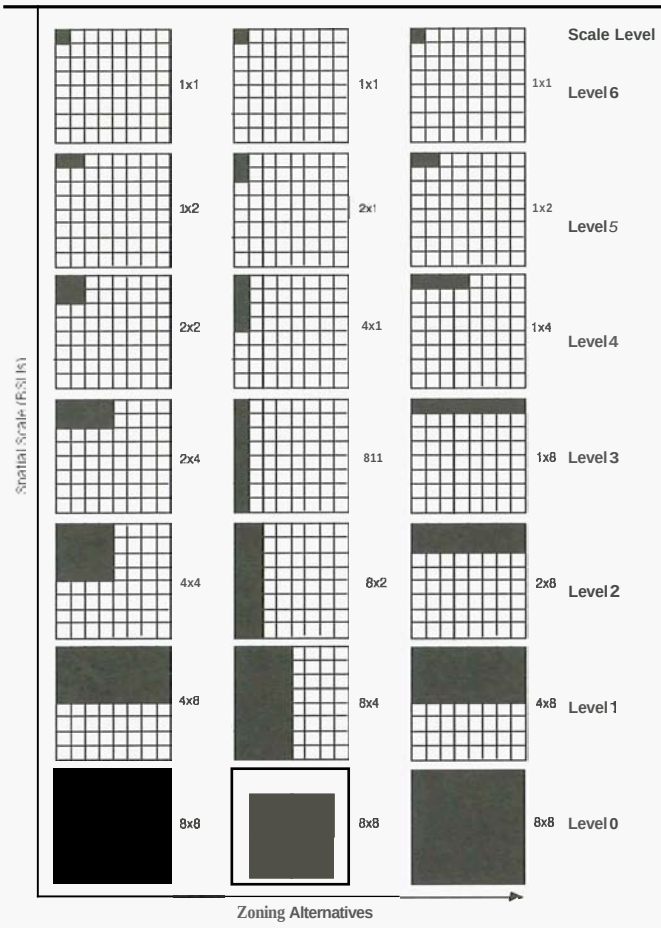


Figure 1. Illustration of spatial aggregation that leads to a spatially nested hierarchy of data. Columns show that the data set becomes coarser and coarser as grain size increases, whereas rows demonstrate that at each grain size there are multiple ways to aggregate the same number of basic spatial units (BSUs) - the pixels in the original fine-resolution data set. The numbers in the figure denote grain sizes (the number of rows x the number of columns of BSUs).

ing formulas:

$$SS_\alpha = \sum_{i=1}^{I}\sum_{j=1}^{J_i}\sum_{k=1}^{K_{ij}}(\bar{X}_{i\bullet\bullet} - \bar{X}_{\bullet\bullet\bullet})^2 \quad (4)$$

$$SS_\beta = \sum_{i=1}^{I}\sum_{j=1}^{J_i}\sum_{k=1}^{K_{ij}}(\bar{X}_{ij\bullet} - \bar{X}_{i\bullet\bullet})^2 \quad (5)$$

$$SS_\gamma = \sum_{i=1}^{I}\sum_{j=1}^{J_i}\sum_{k=1}^{K_{ij}}(X_{ijk} - \bar{X}_{ij\bullet})^2 \quad (6)$$

Dividing the partitioned sums of squares by their respective degrees of freedom results in the corresponding mean square estimates, i.e.:

$$MS_\alpha = \frac{SS_\alpha}{I-1} \quad (7)$$

$$MS_\beta = \frac{SS_\beta}{\sum_{i=1}^{I}(J_i - 1)} \quad (8)$$

$$MS_\gamma = \frac{SS_\gamma}{\sum_{i=1}^{I}\sum_{j=1}^{J_i}(K_{ij} - 1)} \quad (9)$$

When dealing with regular lattice data sets as shown in Figure 1 (Moellering and Tobler's "even case"), the scale variance components are simply:

$$SV_\alpha = MS_\alpha / JK \quad (10)$$

$$SV_\beta = MS_\beta / K \quad (11)$$

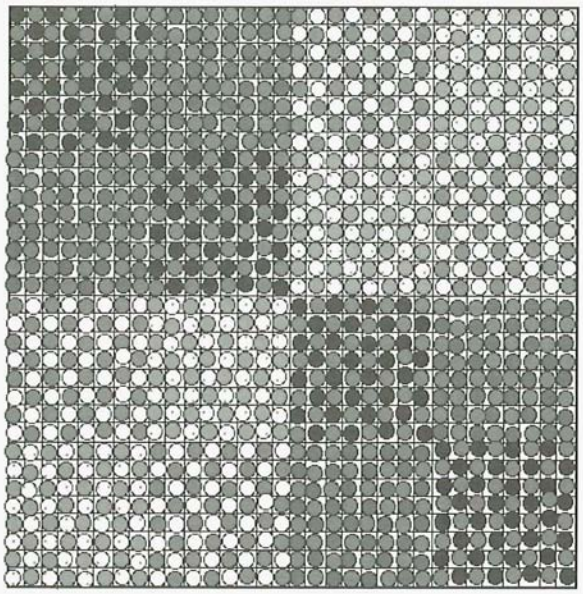
$$SV_\gamma = MS_\gamma \quad (12)$$

Scale variance analysis starts with the construction of nested data hierarchies (Figure 1), and then the above equations are used to compute the total sum of squares, partitioned sums of squares, and scale variance at each scale level. Finally, scale variance or the percent total sum of squares is plotted against scale levels, resulting in the scale variance graph, from which one can readily visualize the presence of peaks or the lack of them. A peak implies that high variability occurs at the corresponding scale level (grain size), which is indicative of the average size of dominant patches in the landscape. The height of the peak reflects the relative contribution of that particular scale level to the total variability of the landscape.

Let's take a look at two simple examples of how scale variance works, and compare it with semivariance analysis. Figure 2 shows two artificially constructed "landscapes" with multiple-scale patterns in which patches of different sizes form spatially nested hierarchies, i.e., larger patches are composed of smaller patches. The left column in Figure 2 is the pictorial version (for facilitating visualization) of the numerical map on the right (actually used in the following analyses). Can scale variance reveal this hierarchical structure? Is it more effective than, say, the simple variance, spatial autocorrelation, and semivariance analysis?

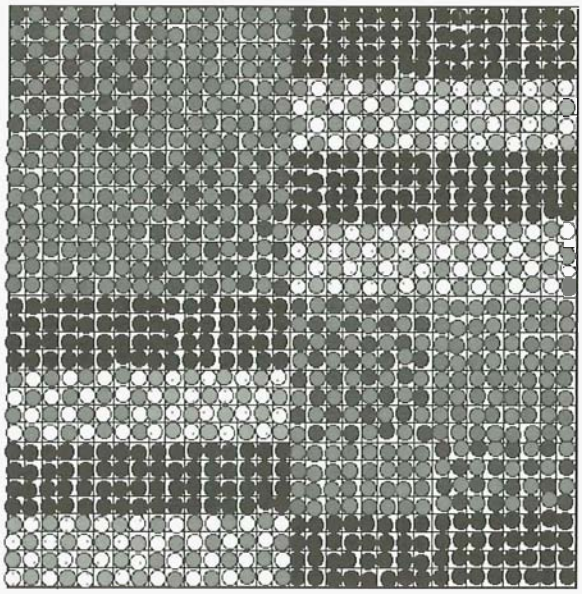
Figure 3 shows that scale variance is indeed able to correctly and clearly identify three peaks corresponding to the three patch sizes (i.e., 1x1, 8x8 and 16x16 BSUs, where BSU stands for the basic spatial unit that is defined as the pixel in the original data set).

PATTERN 1



```
1 4 1 4 1 4 1 4 4 9 4 9 4 9 4 9 3 0 3 0 3 0 3 0 2 7 2 7 2 7 2 7
4 1 4 1 4 1 4 1 9 4 9 4 9 4 9 4 0 3 0 3 0 3 0 3 7 2 7 2 7 2 7 2
1 4 1 4 1 4 1 4 4 9 4 9 4 9 4 4 3 0 3 0 3 0 3 0 2 7 2 7 2 7 2 7
4 1 4 1 4 1 4 1 9 4 9 4 9 4 9 4 0 3 0 3 0 3 0 3 7 2 7 2 7 2 7 2
1 4 1 4 1 4 1 4 4 9 4 9 4 9 4 9 3 0 3 0 3 0 3 0 2 7 2 7 2 7 2 7
4 1 4 1 4 1 4 1 9 4 9 4 9 4 9 4 0 3 0 3 0 3 0 3 7 2 7 2 7 2 7 2
1 4 1 4 1 4 1 4 4 9 4 9 4 9 4 9 3 0 3 0 3 0 3 0 2 7 2 7 2 7 2 7
4 1 4 1 4 1 4 1 9 4 9 4 9 4 9 4 0 3 0 3 0 3 0 3 7 2 7 2 7 2 7 2
4 9 4 9 4 9 4 9 1 4 1 4 1 4 1 4 2 7 2 7 2 7 2 7 3 0 3 0 3 0 3 0
9 4 9 4 9 4 9 4 4 1 4 1 4 1 4 1 7 2 7 2 7 2 7 2 0 3 0 3 0 3 0 3
4 9 4 9 4 9 4 9 1 4 1 4 1 4 1 4 2 7 2 7 2 7 2 7 3 6 3 6 3 8 3 8
9 4 9 4 9 4 9 4 4 1 4 1 4 1 4 1 7 2 7 2 7 2 7 2 0 3 0 3 0 3 0 3
4 9 4 9 4 9 4 9 1 4 1 4 1 4 1 4 2 7 2 7 2 7 2 7 3 0 3 0 3 0 3 0
9 4 9 4 9 4 9 4 4 1 4 1 4 1 4 1 7 2 7 2 7 2 7 2 0 3 0 3 0 3 0 3
4 9 4 9 4 9 4 9 1 4 1 4 1 4 1 4 2 7 2 7 2 7 2 7 3 0 3 0 3 0 3 0
9 4 9 4 9 4 9 4 4 1 4 1 4 1 4 1 7 2 7 2 7 2 7 2 0 3 0 3 0 3 0 3
3 0 3 0 3 0 3 0 2 7 2 7 2 7 2 7 1 4 1 4 1 4 1 4 4 9 4 9 4 9 4 9
0 3 0 3 0 3 0 3 7 2 7 2 7 2 7 2 4 1 4 1 4 1 4 1 9 4 9 4 9 4 9 4
3 0 3 0 3 0 3 0 2 7 2 7 2 7 2 7 1 4 1 4 1 4 1 4 4 9 4 9 4 9 4 9
0 3 0 3 0 3 6 3 7 2 7 2 7 2 7 2 4 1 4 1 4 1 4 1 9 4 9 4 9 4 9 4
3 0 3 0 3 0 3 0 2 7 2 7 2 7 2 7 1 4 1 4 1 4 1 4 4 ~ 4 9 4 ~ 4 ~
0 3 0 3 0 3 0 3 7 2 7 2 7 2 7 2 4 1 4 1 4 1 4 1 9 4 9 4 9 4 9 4
3 0 3 0 3 0 3 8 2 7 2 7 2 7 2 7 1 4 1 4 1 4 1 4 4 9 4 9 4 9 4 9
0 3 0 3 0 3 0 3 7 2 7 2 7 2 7 2 4 1 4 1 4 1 4 1 9 4 9 4 9 4 9 4
2 7 2 7 2 7 2 7 3 0 3 0 3 0 3 0 4 9 4 9 4 9 4 9 1 4 1 4 1 4 1 4
7 2 7 2 7 2 7 2 0 3 0 3 0 3 0 3 9 4 9 4 9 4 9 4 4 1 4 1 4 1 4 1
2 7 2 7 2 7 2 7 3 0 3 0 3 0 3 0 4 9 4 9 4 9 4 9 1 4 1 4 1 4 1 4
7 2 7 2 7 2 7 2 0 3 0 3 0 3 0 3 9 4 9 4 9 4 9 4 4 1 4 1 4 1 4 1
2 7 2 7 2 7 2 7 3 0 3 0 3 0 3 0 4 9 4 9 4 9 4 9 1 4 1 4 1 4 1 4
7 2 7 2 7 2 7 2 0 3 0 3 0 3 0 3 9 4 9 4 9 4 9 4 4 1 4 1 4 1 4 1
2 7 2 7 2 7 2 7 3 0 3 0 3 0 3 0 4 9 4 9 4 9 4 9 1 4 1 4 1 4 1 4
7 2 7 2 7 2 7 2 0 3 0 3 0 3 0 3 9 4 9 4 9 4 9 4 4 1 4 1 4 1 4 1
```

PATTERN 2



```
1 4 1 4 1 4 1 4 4 9 4 9 4 9 4 9 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
4 1 4 1 4 1 4 1 9 4 9 4 9 4 9 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
1 4 1 4 1 4 1 4 4 9 4 9 4 9 4 9 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
4 1 4 1 4 1 4 1 9 4 9 4 9 4 9 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
1 4 1 4 1 4 1 4 4 9 4 9 4 9 4 9 3 0 3 0 3 0 3 0 2 7 2 7 2 7 2 7
4 1 4 1 4 1 4 1 9 4 9 4 9 4 9 4 0 3 0 3 0 3 0 3 7 2 7 2 7 2 7 2
1 4 1 4 1 4 1 4 4 9 4 9 4 9 4 9 3 0 3 0 3 0 3 0 2 7 2 7 2 7 2 7
4 1 4 1 4 1 4 1 9 4 9 4 9 4 9 4 0 3 0 3 0 3 0 3 7 2 7 2 7 2 7 2
4 9 4 9 4 9 4 9 1 4 1 4 1 4 1 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
9 4 9 4 9 4 9 4 4 1 4 1 4 1 4 1 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
4 9 4 9 4 9 4 9 1 4 1 4 1 4 1 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
9 4 9 4 9 4 9 4 4 1 4 1 4 1 4 1 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
4 9 4 9 4 9 4 9 1 4 1 4 1 4 1 4 2 7 2 7 2 7 2 7 3 0 3 0 3 0 3 0
9 4 9 4 9 4 9 4 4 1 4 1 4 1 4 1 7 2 7 2 7 2 7 2 0 3 0 3 0 3 0 3
4 9 4 9 4 9 4 9 1 4 1 4 1 4 1 4 2 7 2 7 2 7 2 7 3 0 3 0 3 0 3 0
9 4 9 4 9 4 9 4 4 1 4 1 4 1 4 1 7 2 7 2 7 2 7 2 0 3 0 3 0 3 0 3
5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 1 4 1 4 1 4 1 4 4 9 4 9 4 9 4 9
5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 4 1 4 1 4 1 4 1 9 4 9 4 9 4 9 4
5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 1 4 1 4 1 4 1 4 4 9 4 9 4 9 4 9
5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 4 1 4 1 4 1 4 1 9 4 9 4 9 4 9 4
3 0 3 0 3 0 3 0 2 7 2 7 2 7 2 7 1 4 1 4 1 4 1 4 4 9 4 9 4 9 4 9
0 3 0 3 0 3 0 3 7 2 7 2 7 2 7 2 4 1 4 1 4 1 4 1 9 4 9 4 9 4 9 4
3 0 3 0 3 0 3 0 2 7 2 7 2 7 2 7 1 4 1 4 1 4 1 4 4 9 4 9 4 9 4 9
0 3 0 3 9 3 0 3 7 2 7 2 7 2 7 2 4 1 4 1 4 1 4 1 9 4 9 4 9 4 9 4
5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 4 9 4 9 4 9 4 9 1 4 1 4 1 4 1 4
5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 9 4 9 4 9 4 9 4 4 1 4 1 4 1 4 1
5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 4 9 4 9 4 9 4 9 1 4 1 4 1 4 1 4
5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 9 4 9 4 9 4 9 4 4 1 4 1 4 1 4 1
2 7 2 7 2 7 2 7 3 6 3 0 3 0 3 0 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
7 2 7 2 7 2 7 2 0 3 0 3 0 3 0 3 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
2 7 2 7 2 7 2 7 3 0 3 0 3 0 3 0 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
7 2 7 2 7 2 7 2 0 3 0 3 0 3 0 3 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
```

Figure 2. Two artificially constructed landscapes that exhibit multiple-scale patterns. The left column is the pictorial version of the numerical map on the right.

Simple variance exhibits a staircase curve, also indicative of a hierarchical structure in the landscape, but not as conspicuous as scale variance (especially for the scale level of 16x16 BSUs). The graph of spatial autocorrelation against scale levels (similar to, but not the same as, a correlogram) also indicates a multiple-scale structure, but is not as easy to interpret as scale variance. Results for the second landscape (pattern 2) for the three methods further support the above observations. Here, three zoning alternatives are used, and in each case scale variance unambiguously reveals two or three hierarchical levels in the data set. Note that changing zoning systems affects the results of all three methods, which is part of MAUP (Jelinski and Wu 1996). At the same time, by knowing how the zones are oriented during the data aggregation, scale variance can provide information on the directionality of dominant elongated patches (see pattern 2 in Figure 2 and the scale variance graph for zoning system 2 in Figure 4).

Figure 5 summarizes the results of a semivariance analysis of these two contrived landscapes. The graph at the top in each column shows that semivariance exhibits cyclic fluctuations, indicative of the periodic pattern in the two landscapes. While this periodicity is not specious, it is difficult to discern whether there exist hierarchical scales in these landscapes and how many from these semivariograms. We also divided the landscapes into four horizontal transects (8x32

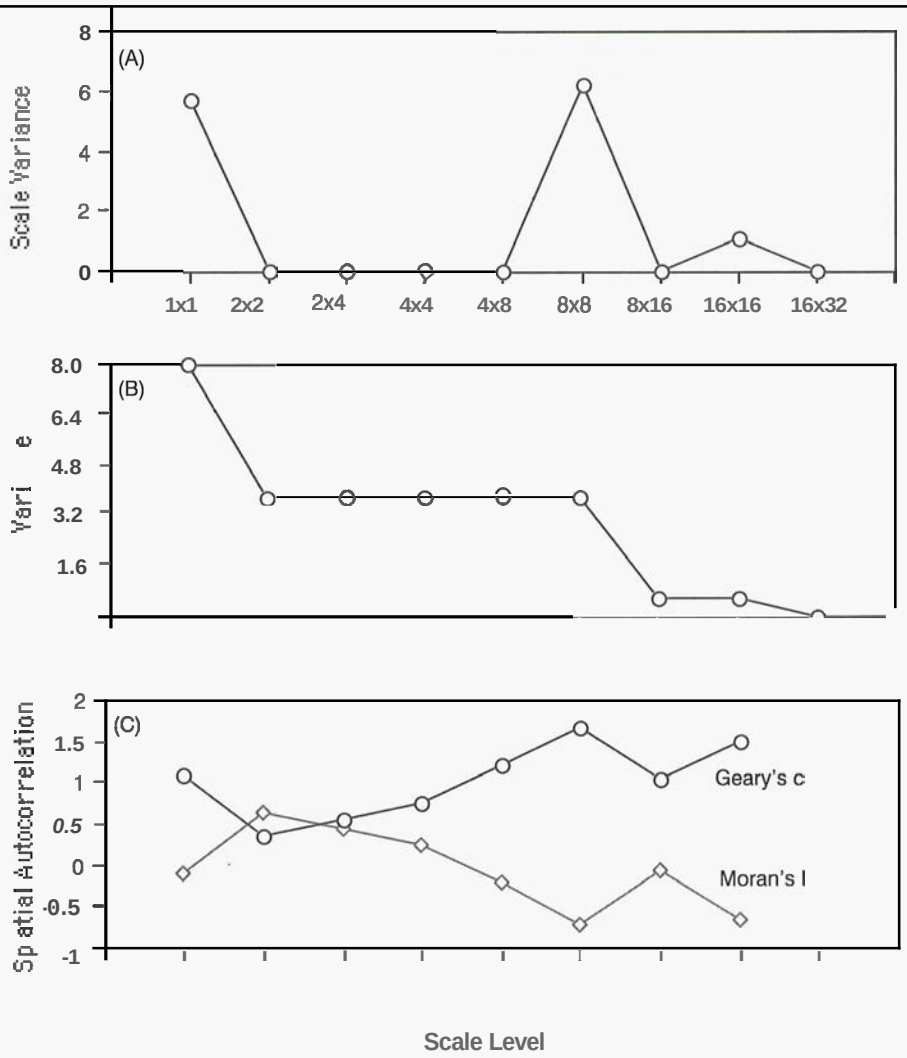


Figure 3. Scale variance analysis of the artificially constructed landscape (pattern **1)** in Figure **2.** Variance and spatial autocorrelation indices are also provided for comparison. The horizontal axis for all three graphs is scale level, representing a hierarchy of grain sizes progressively increasing from **1** by **1** to **16** by **32** BSUs.

pixels each), with transect **1** at the top and transect **4** at the bottom. The semivariogram for the top transect in each landscape seems to indicate a scale break at the lag of 8 pixels, whereas the other three transects exhibit rather similar semivariograms without obvious scale breaks. In all cases, semivariance analysis does not seem to be able to clearly identify the hierarchical levels that apparently exist in the two landscapes. We further compare scale variance with semivariance analysis using a real landscape data set (a map of NDVI, normalized difference vegetation index), with **300x300** pixels each of which has a **30** m linear dimension. The landscape is a boreal forest region, composed of a large number of patches of different vegetation types that vary greatly in size. In Figure ***6,*** scale variance and the percent total sum of squares (top) both show several peaks, indicative of the existence of a multiple-scale structure in the landscape. However, for real landscapes scale variance does not drop to near zero between scale levels, as for the contrived landscapes, because patch sizes may vary continuously, although not evenly; i.e., the nested patch hierarchies are not "neatly" organized. The variance plot (bottom) seems to corroborate this result, but is much less conspicuous. On the other hand, the semivariogram shows that semivariance increases rapidly initially with increasing lags and then gradually levels off (Figure 7). The multiscale structure of the landscape does not become discernable from either the semivariogram for the entire landscape (top) **or for** the three transects (bottom three).

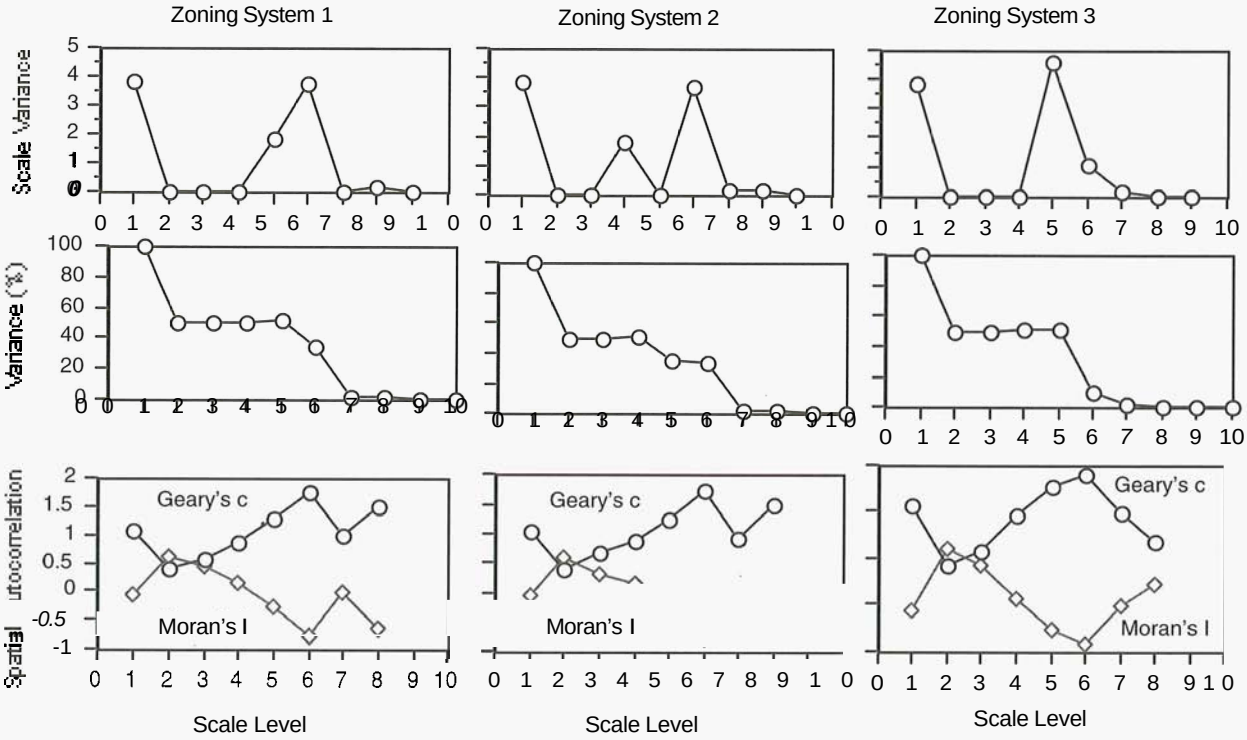
IV. MULTISCALE ANALYSES WITH PATTERN INDICES

The indirect multiscale analysis is closely related to the study of the problem of spatial aggregation in general and MAUP in particular (Wu and Jelinski **1995,** Jelinski and Wu **1996).** Here we focus on the ques-

tion: how different landscape pattern indices respond to systematic changes in grain size as a spatial data set is progressively aggregated with its extent kept constant. We compute a series of landscape metrics using FRAGSTATS (McGarigal and Marks 1995) based on a land cover classification map of an urban-rural-desert landscape in Nevada, USA, occupying an area of 900 km². The classification was conducted using a 1984 Landsat TM scene. The landscape was dominated by different arid vegetation types (e.g., different types of shrublands and woodlands) as well as burned, agricultural, and urban areas.

In total, seventeen commonly used landscape metrics are examined systematically. The total amount of edge, number of patches, edge density, and patch density all show a remarkably consistent power-law relationship with increasing grain size, suggesting that these indices can be predicted over a wide range of grain sizes with high accuracy (the first four graphs in Figure 8). As data become more and more aggregated, the number of patch types (patch richness) and patch diversity (Shannon-Weaver diversity index) both decrease monotonically (the two graphs at the bottom in Figure 8). While the staircase-like decline in patch richness is readily understandable, decreasing patch diversity is a result of the combined decrease in both the number of patch types and the evenness of each type. Comparing patch richness and diversity graphs reveals that the initial rapid decrease in diversity is due to decreasing evenness, whereas later changes in diversity closely resemble those in patch richness. The exact pattern of patch richness and diversity with increasing grain size is determined significantly by the details of landscape heterogeneity (Turner et al. 1989, Wickham and Riitters 1995, Wu et al. 1997).

Contagion index has been widely used to measure the extent to which patches of the same type are clumped (O'Neill et al. 1988, Li and Reynolds 1993, Riitters et al. 1996). One may expect that contagion should in-



Scale Level		1	2	3	4	5	6	7	8	9	10	Unit
Grain Size (for 3 Zoning Systems)	1	1x1	2x2	2x4	4x4	4x8	8x8	8x16	16x16	16x32	32x32	(BSUs/grain)
	2	1x1	2x2	4x2	4x4	8x4	8x8	16x8	16x16	32x16	32x32	(BSUs/grain)
	3	1x1	2x2	2x4	2x8	4x8	4x16	8x16	8x32	16x32	32x32	(BSUs/grain)

Figure 4. Scale variance graph (top row) of the artificially constructed landscape (pattern 2) in Figure 2. Variance (middle row) and spatial autocorrelation indices (bottom row) are provided for comparison. Three columns represent three different zoning alternatives. The horizontal axis for all graphs is scale level, representing a nested hierarchy of grain sizes.

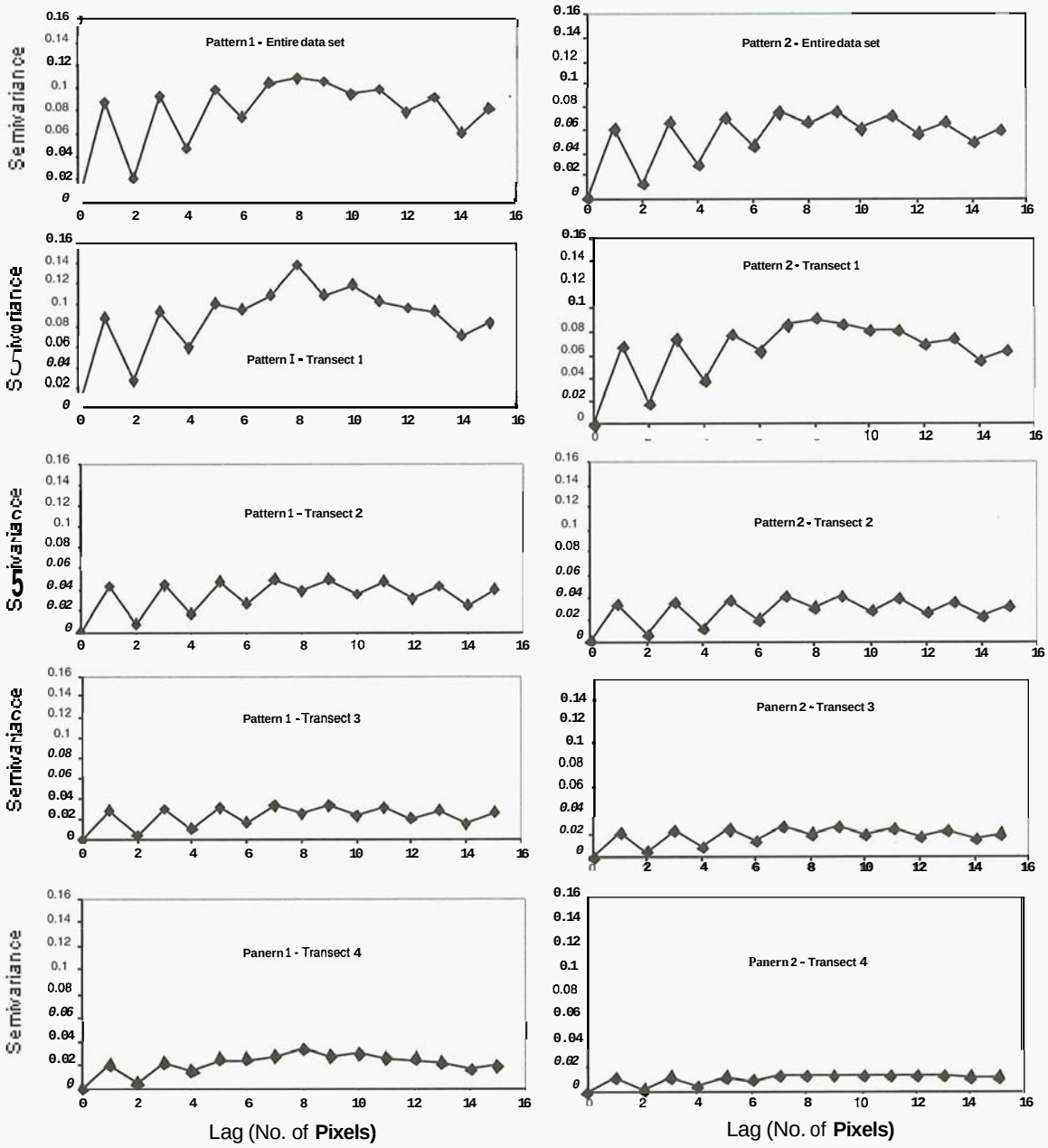


Figure 5. Semivariance analysis of the artificially constructed landscape (pattern 1, left column; pattern 2, right column) in Figure 2. The top graph in each column is for the entire landscape, and the other four represent four evenly divided horizontal transects from top to bottom (8x32 BSUs each).

crease monotonically with increasing grain size simply because of the progressive agglomeration of smaller patches into larger ones of the same type. However, this is not the case here. Figure 9 shows that contagion increases up to a certain grain size and then begins to decline. In fact, for a given spatial pattern a finer grain size renders a larger contagion (Frohn 1998). Because several factors, including patch diversity, spatial pattern, and grain size, together affect the value of contagion (see Li and Reynolds 1993, Riitters et al. 1996), it is difficult, if meaningful, to interpret its response curve. Square pixel index (Frohn 1998) and landscape shape index are both derived from the perimeter-area ratio. **As** grain size increases, landscape shape index decreases rapidly following a power law, whereas square pixel, a normalized shape index, decreases linearly (Figure 9). In contrast with the assertions by Frohn (1998), the insensitivity of square pixel to changing grain size suggests that it may not be a good measure for detecting changes in landscape shape complexity across scales or along a gradient (also see Wu in review). The fractal dimension of the landscape remains constant over a range of grain sizes, which may suggest self-similar-

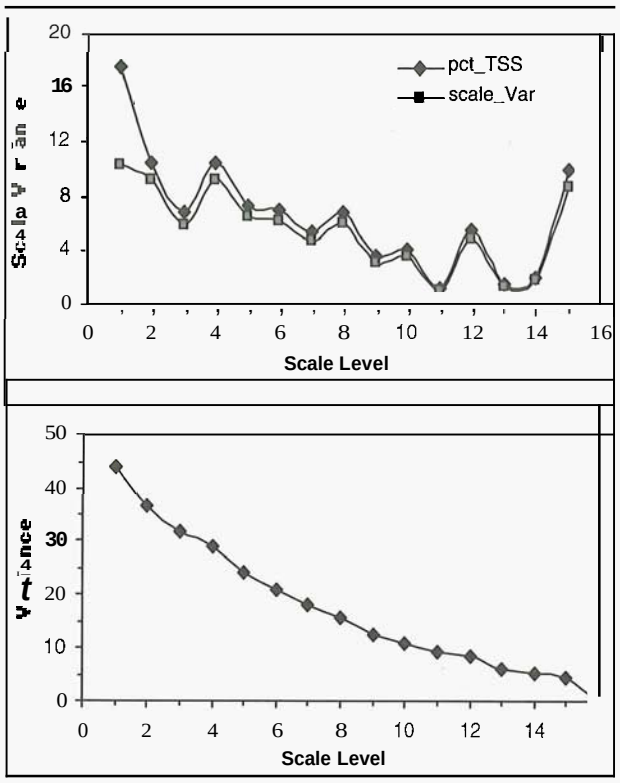


Figure 6. Scale variance graph (top) showing the multiple-scale structure of a boreal forest landscape in northern Canada. Also plotted along with scale variance is the percent total sum of squares. Variance at each scale level is also shown for comparison (bottom).

ity, and then begins to fluctuate after grain size exceeds 50 pixels on a side. Together with contagion, the landscape fractal graph may be indicative of different landscape features emerging over coarse grain sizes. These features are more than likely "spatial" because the non-spatial measures, like landscape shape index and square pixel index, do not pick up this information (Figure 9).

Figure 10 shows the response curves of mean patch size (MPS), patch size coefficient of variation (PSCV), mean patch fractal dimension (MPFD), area-weighted mean patch fractal dimension (AWMFD), patch size standard deviation (PSSD), mean patch shape index (MSI), and area-weighted mean patch shape index (AWMSI). It is trivial to speculate that MPS will increase with increasing grain size in any landscape. Yet, it is interesting to note that the increase in MPS is readily predictable and that its pattern seems to indicate multiple-scale patterns existing at grain sizes of about 60x60 and 80x80 pixels. This scale multiplicity in landscape pattern again is noticeable in the response curves of AWMFD, PSSD, MSI, and AWMSI (Figure 10). While patch size standard deviation in-

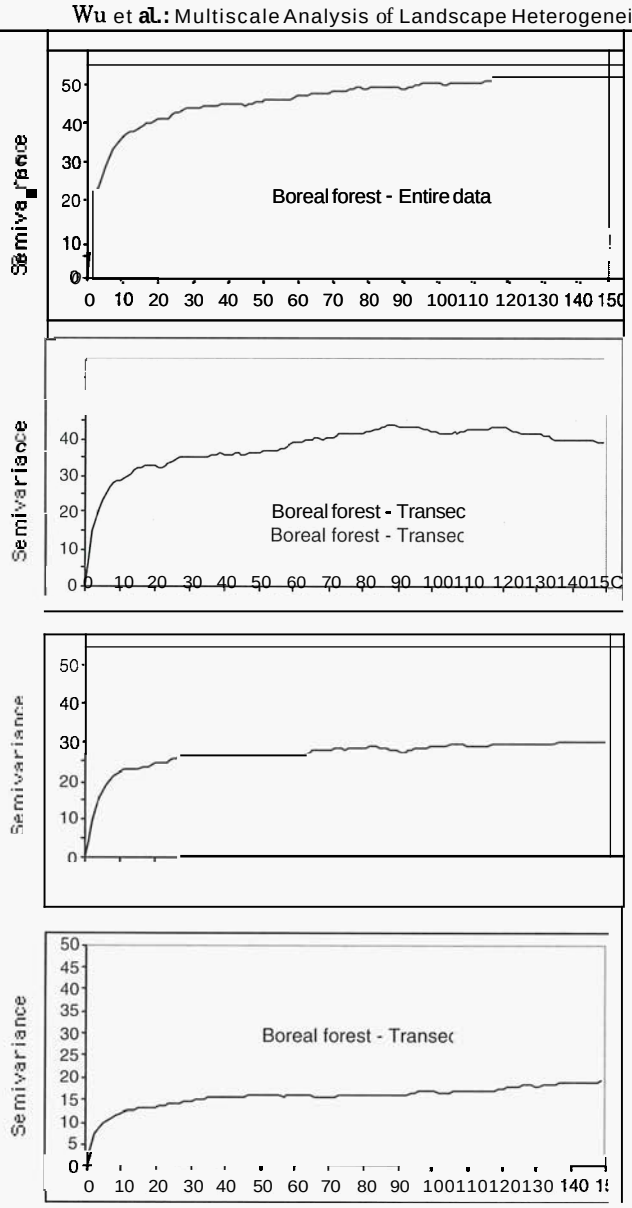


Figure 7. Semivariogram for a boreal forest landscape in northern Canada. The top graph is for the entire data set (300 x 300 pixels), and the lower three graphs are for three consecutive west-east transects (each 100 x 300 pixels) from north to south, respectively.

creases almost linearly with increasing grain size, patch size coefficient of variation, i.e., patch size standard deviation divided by mean patch size, decreases again in a power-law fashion (Figure 10). Mean patch fractal dimension does not change notably with grain size, but area-weighted mean patch fractal dimension demonstrates a rapid nonlinear decline which is similar to that of area-weighted mean patch shape index. Also noticeable is mean patch shape index which seems sensitive to changing grain size, and thus may be used together with MPS, AWMFD, PSSD, and AWMSI to detect, in addition to describing, multiscale patterns in landscapes.

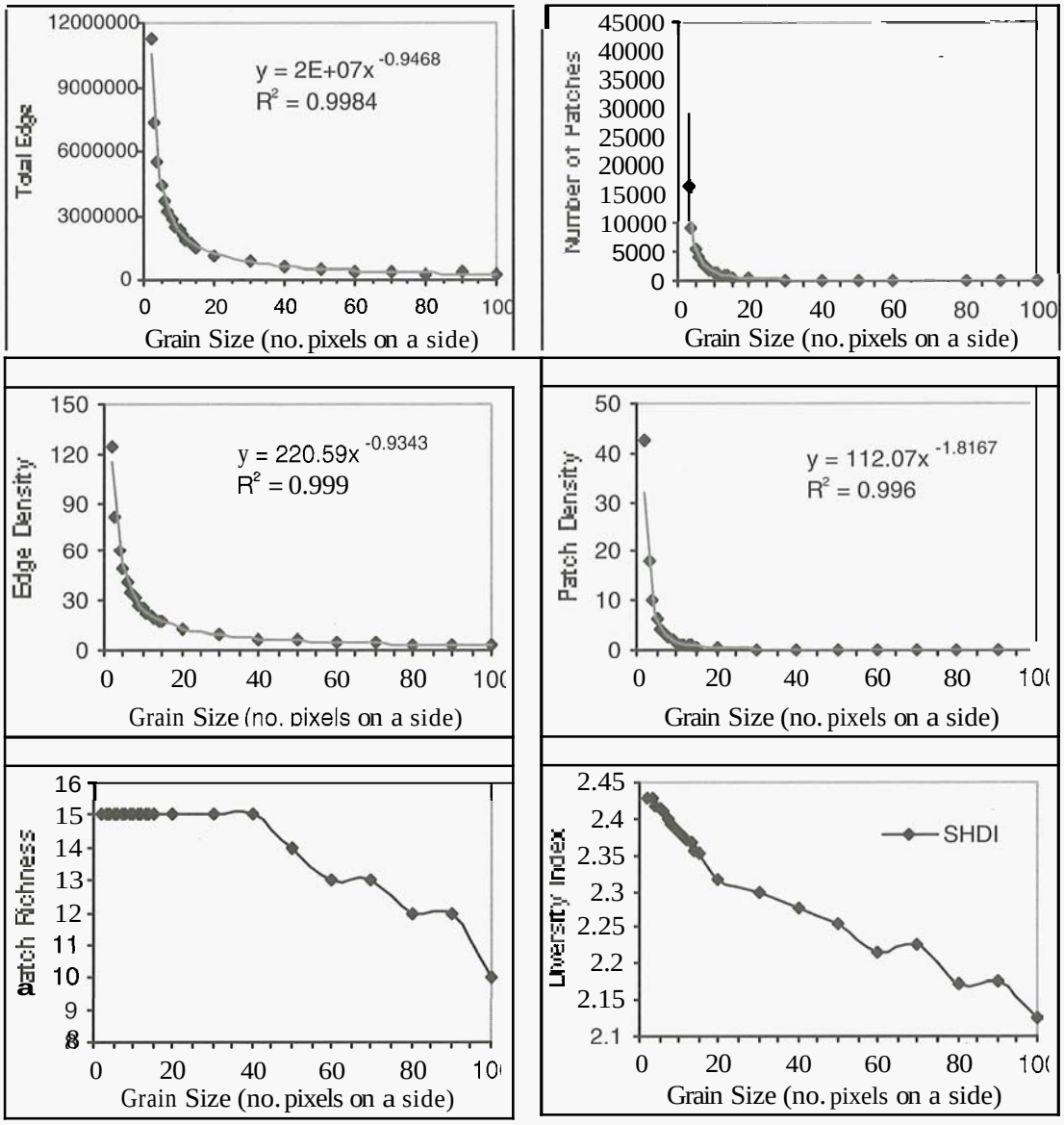


Figure 8. Response curves of landscape metrics to progressively increasing grain size: total edge, number of patches, edge density, patch density, patch richness, and Shannon diversity index.

V. DISCUSSION AND CONCLUSIONS

The relationship between pattern and scale is extremely intriguing and important in ecology (Levin 1992), but remains elusive even when pattern is restricted to spatial pattern and scale to grain and extent. Detecting, describing and understanding the multiple-scale structure of spatial heterogeneity are essential in landscape ecology, or more appropriately, spatial ecology. Although many methods have been used to achieve this goal in landscape ecology since the 1980s, the effectiveness of even the most widely used methods (e.g., correlograms, variograms) remains unclear or questionable.

In this paper, we outline two complementary, yet parallel approaches to multiscale analysis of landscape pattern: the direct approach that uses multiscale statistical methods and the indirect approach that usually employs simple synoptic pattern indices with hierarchically resampled data. In particular, we illustrate the use of scale variance analysis with contrived landscape data as well as a real landscape data set. Semivariance analysis and spatial autocorrelation analysis are used for the purpose of comparison. The results show that scale variance analysis seems to be a more robust method for detecting and describing multiple-scale or hierarchical structures of landscapes. Townshend and Justice (1988, 1990) have shown that scale variance analysis is just as powerful as complicated methods such as spectral analysis, but much

simpler in computation and much more transparent in interpretation. Although semivariance analysis has been claimed as one of the most effective methods for detecting the multi-scale or hierarchical structure of landscapes, our results here suggest that this may not always be true. In semivariograms of real landscapes, fine-scale variability can be "squeezed" by broad-scale variability, which makes it less likely for a clearly identifiable staircase curve (e.g., Robertson and Gross **1994)** to emerge. Meisel and Turner **(1998)** also pointed out that, although semivariance analysis did reveal the hierarchical structure in their artificial maps, it is unlikely to detect multiscale patterns in real landscapes.

The results of our multiscale analysis with seventeen commonly used landscape pattern metrics show that almost all of them change considerably with increasing grain size. These changes reflect the notorious problem known as MAUP and, at least sometimes, the multiple-scale structure in landscape pattern. Some metrics (e.g., the number of patches, patch density, total edge, edge density, mean patch size, patch size coefficient of variation) seem to exhibit consistent patterns over a wide range of grain sizes, and thus can be predicted accurately with simple regression equations. On the other hand, nonlinear response curves are found for other metrics (e.g., patch diversity, contagion, landscape fractal dimension). It makes little sense to characterize landscape pattern with any of these indices at a single scale, be it grain or extent. While a multiple-scale analysis with several landscape metrics across scales is necessary for meaningfully describing landscape pattern, doing so can also render valuable information on detecting possible scale multiplicity in the pattern.

All spatial data and all types of spatial analysis carry errors of one sort or another (Fotheringham **1989).** The usefulness of a spatial study may be critically affected by the nature and the intrinsic meaningfulness of the objects or units in the data set (Openshaw **1984).** The multiple-scale analyses discussed here are intimately related to the problem of spatial aggregation in statistics and human geography in general. Specifically, MAUP may have significant influences on the detection of scale, the determination of relationships among organizational levels, and the translation of information across scales. Indeed, the modifiable areal unit problem suggests that results of many past ecological studies based on spatially aggregated data may be flawed or seriously biased and, therefore, should be reexamined. There is apparently a lack of awareness of the vast literature on MAUP in

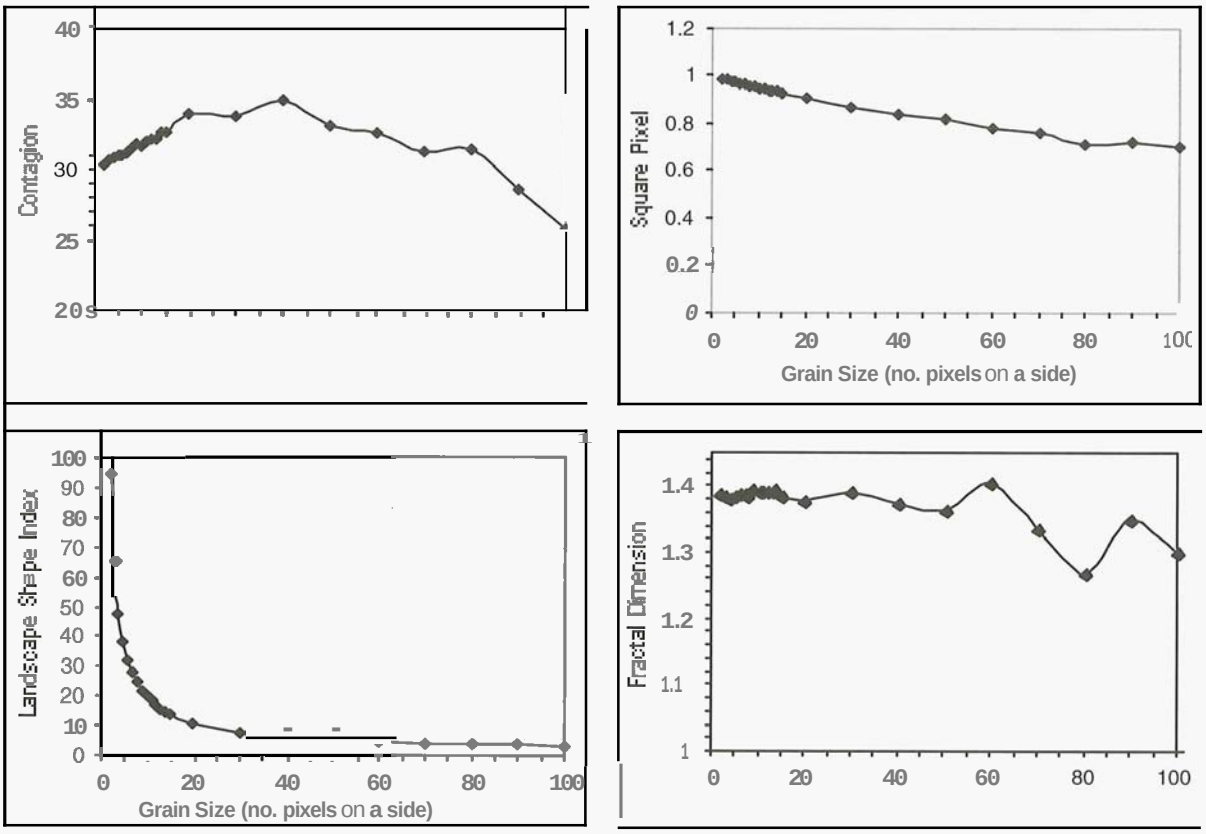


Figure 9. Response curves of landscape metrics to progressively increasing grain size: contagion, square pixel index, landscape shape index, and landscape fractal dimension.

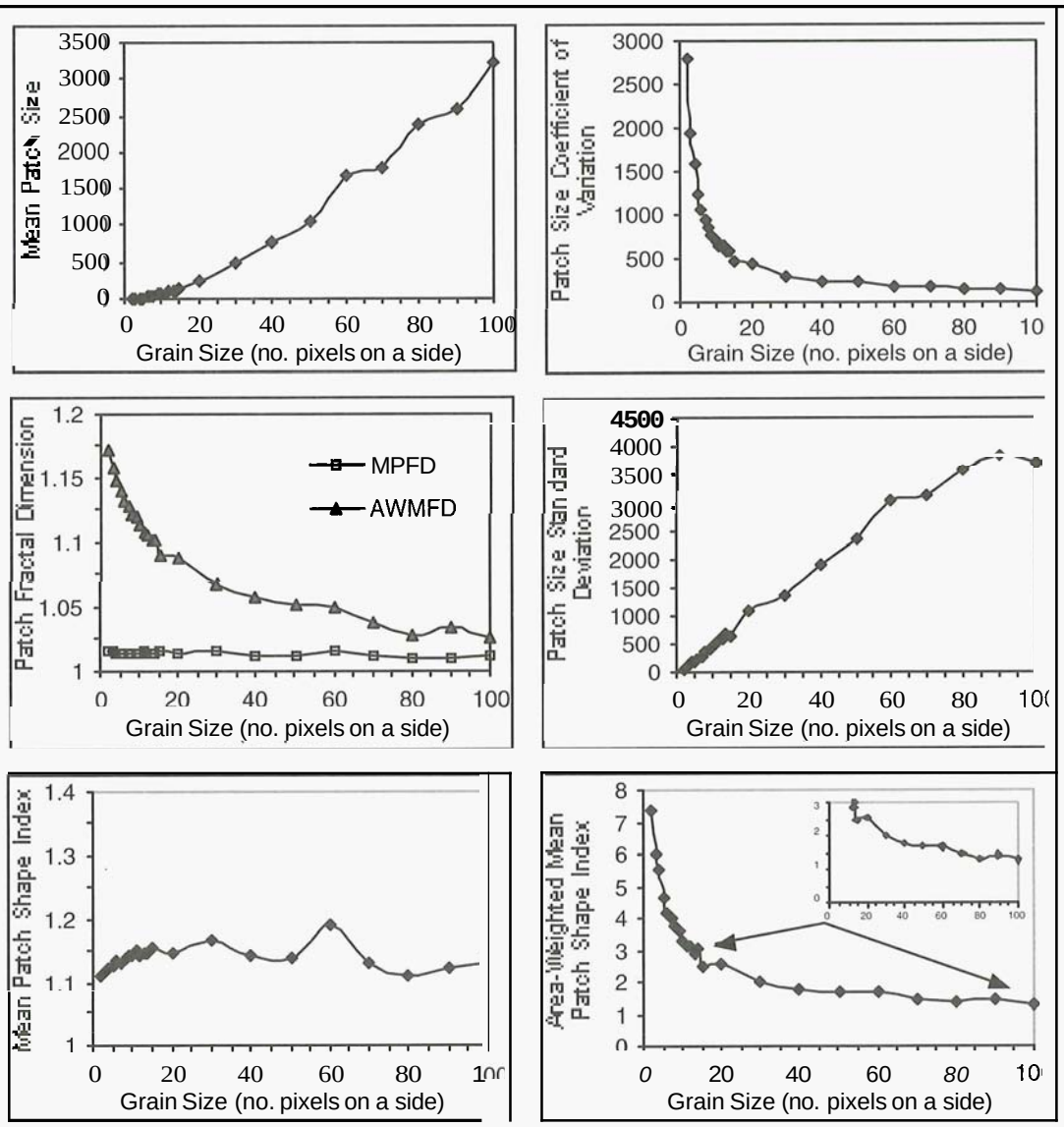


Figure 10. Response curves of landscape metrics to progressively increasing grain size: mean patch size, patch size coefficient of variation, patch fractal dimension, patch size standard deviation, mean patch shape index, and area-weighted mean patch shape index.

the ecology community, and ecologists should make a conscious effort to integrate into their own understanding of pattern and scale the valuable information on the issue of scale in geography and social sciences (Marceau 1999, Wu and Qi this issue).

To understand the role of scale in studying spatial heterogeneity, three related but distinctive groups of research questions must be adequately addressed: **(1)** How does changing the scale of observation or analysis affect research results and their interpretation, and are these changes predictable? (2) Are ecological systems multiple-scaled or hierarchically structured, and if so, how do we identify and interpret characteristic scales in relation to patterns and processes in a landscape? **(3)** What scaling laws exist for different patterns and processes in landscapes that are heterogeneous in various ways? In the case of no simple and mathematically tractable scaling laws, how do we develop systematic procedures to guide the translation or extrapolation of information from one scale to another? The results of our study shed light on these issues. However, these research questions may remain among the most essential and the most challenging in landscape ecology for a long time, and full answers to them dictate further continuing theoretical and empirical studies.

ACKNOWLEDGMENTS

This research was in part supported by USDA NRICGP grant 95-37101-2028 (to PTT and JW), NSF grant DEB 97-14833 (CAP-LTER), and US EPA grant R827676-01-0 (to JW). Although the research described in this article has been funded in part by the above mentioned agencies, it has not been subjected to the Agencies' required peer and policy review and therefore does not necessarily reflect the views of the agencies and no official endorsement should be inferred. We thank John David, Cindy Overton and Weijun Shen for their comments on the manuscript.

REFERENCES

[1] Barnsley, M. J., S. L. Barr, and T. T. 1997. Scalingand generalisation in land cover mapping from satellite sensors. Pages 173-199 in P. R. van Gardingen, G. M. Foody, and P. J. Curran, editors. ***Scaling-up From Cell To Landscape.*** Cambridge University Press, New York.

[2] Bradshaw, G. A., and T. A. Spies. 1992. Characterizing canopy gap structure in forests using wavelet analysis. ***Journal of Ecology,*** 80:205-215.

[3] Burrough, P. A. 1995. Spatial aspects of ecological data. Pages 213-265 in R. H. G. Jongman, C. J. F. Ter Braak, and v. T. F. R., editors. ***Data Analysis in Community and Landscape Ecology.*** Cambridge University Press, Cambridge.

[4] Cullinan, V. I., M. A. Simmons, and J. M. Thomas. 1997. A Bayesian test of hierarchy theory: Scaling up variability in plant cover from field to remotely sensed data. ***Landscape Ecology,*** 12:273-285.

[5] Dale, M. R. T. 1999. ***Spatial Pattern Analysis in Plant Ecology.*** Cambridge University Press, Cambridge.

[6] Fortin, M. J. 1999. Spatial statistics in landscape ecology. Pages 253-279 in J. M. Klopatek and R. H. Gardner, editors. ***Landscape Ecological Analysis: Issues adn Applications.*** Springer-Verlag, New York.

[7] Fotheringham, S. 1989. Scale-independent spatial analysis. Pages 221-228 in M. F. Goodchild and S. Gopal, editors. ***Accuracy of Spatial Databases.*** Taylor and Francis, London.

[8] Frohn, R. C. 1998. ***Remote Sensing for Landscape Ecology: New Metric Indicators for Monitoring, Modeling, and Assessment of Ecosystems.*** Lewis Publishers, Boca Raton.

[9] Greig-Smith, P. 1983. ***Quantitative Plant Ecology.*** University of California Press, Berkeley.

[10] Gustafson, E. J. 1998. Quantifying landscape spatial pattern: What is the state of the art? ***Ecosystems,*** 1:143-156.

[11] Henebry, G. M., and H. J. H. Kux. 1995. Lacunarity as a texture measure for SAR imagery. ***International Journal of Remote Sensing,*** 16:565-571.

[12] Jelinski, D. E., and J. Wu. 1996. The modifiable areal unit problem and implications for landscape ecology. ***Landscape Ecology,*** 11:129-140.

[13] Kolasa, J., and S. T. A. Pickett, editors. 1991. ***Ecological Heterogeneity.*** Springer-Verlag, New York.

[14] Krummel, J. R., R. H. Gardner, G. Sugihara, R. V. O'Neill, and P. R. Coleman. 1987. Landscape patterns in a disturbed environment. ***Oikos,*** 48:321-324.

[15] Legendre, P. 1993. Spatial autocorrelation: Trouble or new paradigm? ***Ecology,*** 74:1659-1673.

[16] Legendre, P., and M.-J. Fortin. 1989. Spatial pattern and ecological analysis. Vegetatio 80:107-138.

[17] Levin, S. A. 1992. The problem of pattern and scale in ecology. ***Ecology,*** 73:1943-1967.

[18] Li, H., and J. F. Reynolds. 1993. A new contagion index to quantify spatial patterns of landscapes. Landscape ***Ecology,*** 8: 155-162.

[19] Marceau, D. J. 1999. The scale issue in social and natural sciences. ***Canadian Journal of Remote Sensing,*** 25:347-356.

[20] McGarigal, K., and B. J. Marks. 1995. ***FRAGSTATS: Spatial Pattern Analysis Program for Quantifying Landscape Structure. Gen. Tech. Rep.*** PNW-GTR-351. Pacific Northwest research Station, USDA-Forest Service, Portland.

[21] Meisel, J. E., and M. G. Turner. 1998. Scale detection in real and artificial landscapes using semivariance analysis. ***Landscape Ecology,*** 13:347-362.

[22] Miller, D. H. 1978. The factor of scale: Ecosystem, landscape mosaic, and region. Pages 63-88 in K. A. Hammond, G. Macinio and W.B. Fairchild, editor. ***Sourcebook on the Environment: A Guide to the Literature.*** University of Chicago Press, Chicago.

[23] Milne, B. T. 1991. Lessons from Applying Fractal Models to Landscape Patterns. Pages 199-235 in M. G. a. R. H. G. Turner, editor. ***Quantitative Methods in Landscape Ecology.*** Springer-Verlag, ***NY.***

[24] Moellering, H., and W. Tobler. 1972. Geographical variances. Geographical Analysis 4:34-64.

[25] Nikora, V. I., C. P. Pearson, and U. Shankar. 1999. Scaling properties in landscape patterns: New Zealand experience. ***Landscape Ecology,*** 14:17-33.

[26] O'Neill, R. V., D. L. DeAngelis, J. B. Waide, and T. F. H. Allen. 1986. ***A Hierarchical Concept of Ecosystems.*** Princeton University Press, Princeton.

[27] O'Neill, R. V., R. H. Gardner, B. T. Milne, M. G. Turner, and B. Jackson. 1991. Heterogeneity and Spatial Hierarchies. Pages 85-96 in J. Kolasa and S. T. A. Pickett, editors. ***Ecological Heterogeneity.*** Springer-Verlag, New York.

[28] O'Neill, R. V., B. T. Milne, M. G. Turner, and R. H. Gardner. 1988. Resource utilization scales and landscape pattern. Landscape Ecology 2:63-69.

[29] Openshaw, S. 1984. ***The Modifiable Areal Unit Problem.*** Geo Books, Norwich.

[30] Platt, T., and K. L. Denman. 1975. Spectral analysis in ecology. ***Ann. Rev. Ecol. Syst.*** 6:189-210.

[31] Plotnick, R. E., R. H. Gardner, and R. V. O'Neill. 1993. Lacunarity indices as measures of landscape texture. ***Landscape Ecology,*** 8:201-211.

[32] Riitters, K. H., R. V. O'Neill, J. D. Wickham, and K. B. Jones. 1996. A note on contagion indices for landscape

analysis. Landscape Ecology 11:197-202.

[33] Ripley, B. D. 1978. Spectral analysis and the analysis of pattern in plant communities. *Journal of Ecology,* 66:965-981.

[34] Robertson, G. P. 1987. Geostatistics in ecology: Interpolating with known variance. *Ecology,* 68:744-748.

[35] Robertson, G. P., and K. L. Gross. 1994. Assessing the heterogeneity of belowground resources: Quantifying pattern and scale. Pages 237-253 in M. M. Caldwell and R. W. Pearcy, editors. *Exploitation of Environmental Heterogeneity by Plants :Ecophysiological Processes Above- and Belowground.* Academic Press, San Diego.

[36] Rossi, R. E., D. J. Mulla, A. G. Journel, and E. H. Franz. 1992. Geostatistical tools for modeling and interpreting ecological spatial dependence. *Ecological Monographs,* 62:277-314.

[37] Saunders, S. C., J. Chen, T. R. Crow, and K. D. Brosofske. 1998. Hierarchical relationships between landscape structure and temperature in a managed forest landscape. *Landscape Ecology,* 13:381-395.

[38] Townshend, J. R. G., and C. O. Justice. 1988. Selecting the spatial resolution of satellite sensors required for global monitoring of land transformations. *Int. J. Remote Sensing,* 9:187-236.

[39] Townshend, J. R. G., and C. O. Justice. 1990. The spatial variation of vegetation changes at very coarse scales. *Int. J. Remote Sensing,* 11:149-157.

[40] Turner, S. J., R. V. O'Neill, W. Conley, M. R. Conley, and H. C. Humphries. 1991. Pattern and scale: Statistics for landscape ecology. Pages 17-49 in M. G. Turner and R. H. Gardner, editors. *Quantitative Methods in Landscape Ecology.* Springer-Verlag, New York.

[41] Turner, M. G., R. V. O'Neill, R. H. Gardner, and B. T. Milne. 1989. Effects of changing spatial scale on the analysis of landscape pattern. *Landscape Ecology,* 3:153-162.

[42] van Gardingen, P. R., G. M. Foody, and P. J. Curran, editors. 1997. *Scaling-Up: From Cell to Landscape.* Cambridge University Press, Cambridge.

[43] Werner, B. T. 1999. Complexity in natural landform patterns. Science 284:102-104.

[44] Wickham, J. D., and K. H. Riitters. 1995. Sensitivity of landscape metrics to pixel size. *International Journal of Remote Sensing,* 16:3585-3595.

[45] Wu, J. 1999. Hierarchy and scaling: Extrapolating information along a scaling ladder. *Canadian Journal of Remote Sensing,* 25:367-380.

[46] Wu, J. 2000. Pattern and scale: The behavior of landscape metrics. in review.

[47] Wu, J., W. Gao, and P. T. Tueller. 1997. Effects of changing spatial scale on the results of statistical analysis with landscape data: A case study. *Geographic Information Sciences,* 3:30-41.

[48] Wu, J., and D. E. Jelinski. 1995. Pattern and scale in ecology: The modifiable areal unit problem. Pages 1-9 in B. Li, editor. *Lectures in Modern Ecology.* Science Press, Beijing.

[49] Wu, J., D. E. Jelinski, and Y. Qi. 1994. Spatial pattern analysis of a boreal forest landscape: scale effects and interpretation. Pages 165 in *Proceedings of the VI International Congress of Ecology,* Manchester, UK.

[50] Wu, J., and S. A. Levin. 1994. A spatial patch dynamic modeling approach to pattern and process in an annual grassland. *Ecological Monographs,* 64(4):447-464.

[51] Wu, J., and O. L. Loucks. 1995. From balance-of-nature to hierarchical patch dynamics: A paradigm shift in ecology. *Quarter Review of Biology,* 70:439-466.

[52] Wu, J., and Y. Qi. 2000. Dealing with scale in landscape analysis: An overview. *Geographic Information Sciences,* 6:1-5.